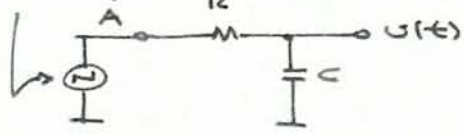


$v_{in}(t) = A \sin(\omega t)$ $u(t)$



$\frac{d(q = Cv)}{dt} \rightarrow i = C \frac{dv}{dt}$

$v(t) + RC \frac{dv(t)}{dt} = v_{in}(t)$

$v(t) \Big|_{t=0} = 0$

① $v_h(t) = k e^{-t/RC}$

$v_h(t) + RC \frac{dv_h(t)}{dt} = 0$
 $k e^{-t/RC} - \frac{k(RC)}{RC} e^{-t/RC} = 0 \quad (\checkmark)$

② $v_p(t) = G e^{j\omega t}$ $\leftarrow v_p(t) + RC \frac{dv_p(t)}{dt} = e^{j\omega t}$

$G e^{j\omega t} + j\omega RC G e^{j\omega t} = e^{j\omega t}$
 $G + j\omega RC G = 1$
 $G = \frac{1}{1 + j\omega RC} = \frac{1}{\sqrt{1 + (\omega RC)^2}} e^{j\phi}$; $\phi = -\arctan(\omega RC)$

Da mesma forma:
 $v_p(t) + RC \frac{dv_p(t)}{dt} = e^{-j\omega t} \rightarrow v_p(t) = H e^{-j\omega t}$
 $H e^{-j\omega t} - j\omega RC H e^{-j\omega t} = e^{-j\omega t}$
 $H = \frac{1}{1 - j\omega RC} = \frac{1}{\sqrt{1 + (\omega RC)^2}} e^{-j\phi}$; $\phi = -\arctan(\omega RC)$

Considerando entrada senoidal:

$v_{in}(t) = A (e^{j\omega t} - e^{-j\omega t})$

Saida: $\frac{A}{\sqrt{1 + (\omega RC)^2}} \frac{(e^{j\phi} e^{j\omega t} - e^{-j\phi} e^{-j\omega t})}{2j} = v_p(t)$

$v_p(t) = \frac{A}{\sqrt{1 + (\omega RC)^2}} \sin(\omega t + \phi) = B \sin(\omega t + \phi)$

③ Solução completa (homogênea + particular):

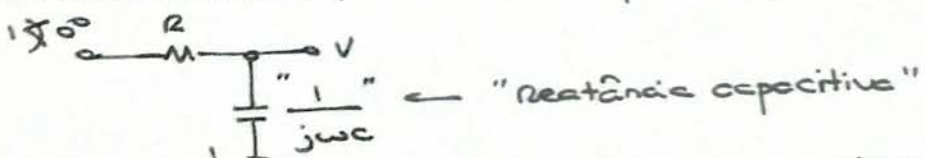
$v(t) = k e^{-t/RC} + B \sin(\omega t + \phi)$

$t=0 \rightarrow v(0)=0 \rightarrow k + B \sin(\phi) = 0 \rightarrow k = -B \sin \phi$

Ex.: $R = 18 \text{ k}\Omega$; $C = 22 \text{ nF}$ (18 "kilo ohms", 22 "nano farads")

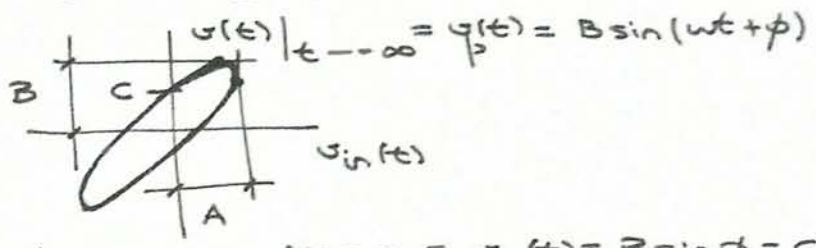
$f = 400 \text{ Hz}$
 $\omega = \frac{1}{RC} = 1 \text{ rad/seg} \rightarrow 1 + \omega RC = 2 \rightarrow B = \frac{A}{\sqrt{2}}$; $\phi = -45^\circ$

Alternativamente ("método dos fasores"):



$\frac{V}{1 \angle 0^\circ} = \frac{1/j\omega C}{R + 1/j\omega C} \rightarrow V = \frac{1}{1 + j\omega RC}$ $\rightarrow v(t) = B \sin(\omega t + \phi)$
 $B = |V|$; $\phi = \angle V$

Figuras de Lissajous:



$v(t) \Big|_{t \rightarrow -\infty} = v_p(t) = B \sin(\omega t + \phi)$

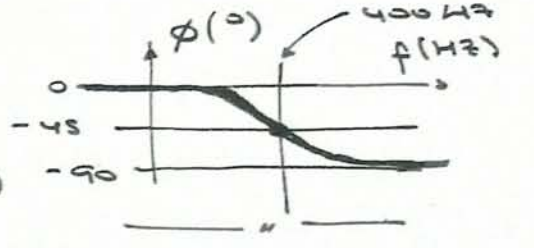
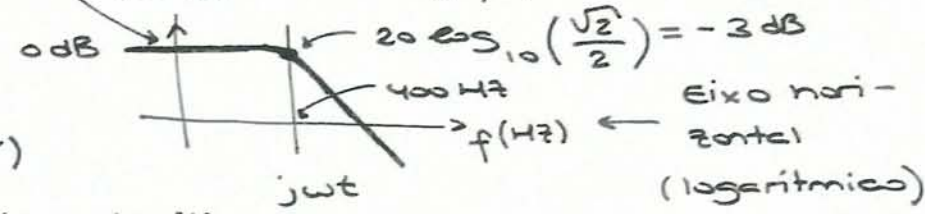
"Ganho" da resposta do filtro: $\frac{B}{A}$

\hookrightarrow Em dB: $20 \log_{10} \left(\frac{B}{A} \right)$

"fase" da resposta do filtro: $\phi = B \sin \phi$

$\phi = \arcsin\left(\frac{C}{B}\right)$

$20 \log_{10} \left(\frac{B}{A} \right)$ Google: "semilog paper"



Observação:

Considere $z = 1 + j$

Módulo de z : $|z| = \sqrt{2}$

Fase de z : $\arctan(1) = 45 \text{ graus}$

$1/z = 1 / (1+j) = (1-j) / 2$

Módulo de $1/z$: $|1/z| = \sqrt{2}/2$

Note que o módulo de $1/z$ é igual a $1/|z|$

Fase de $1/z$: $\arctan(-1) = -45 \text{ graus}$

Note que a fase de $1/z$ é igual a $- \text{fase}(z)$