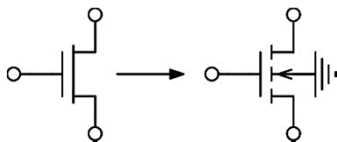
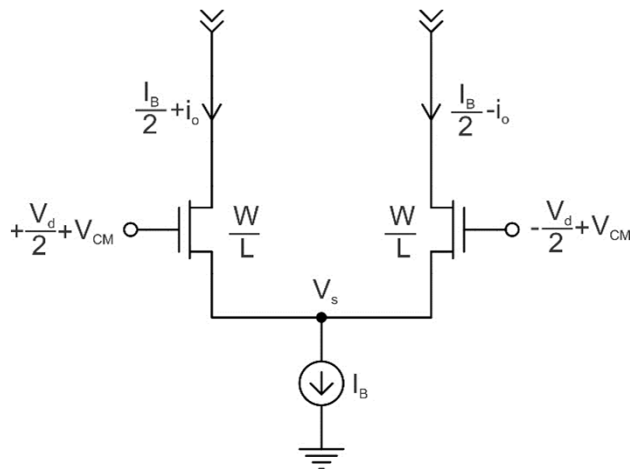


Amplificador Diferencial

Os amplificadores diferenciais são blocos básicos na construção de Amplificadores Operacionais (OpAmp), Amplificadores Operacionais de Transcondutância (OTA), comparadores de tensão, moduladores, osciladores, etc...

Par diferencial tipo N – Inversão Forte

Saturação



Equações do circuito

$$\beta = k_p \frac{W}{L}$$

$$\frac{I_B}{2} + i_0 = \frac{\beta}{2\alpha} \left(\frac{v_d}{2} + V_{CM} - v_s - V_T \right)^2$$

$$\frac{I_B}{2} - i_0 = \frac{\beta}{2\alpha} \left(-\frac{v_d}{2} + V_{CM} - v_s - V_T \right)^2$$

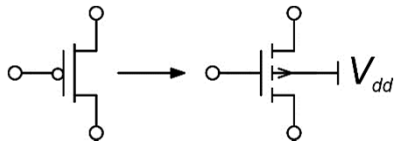
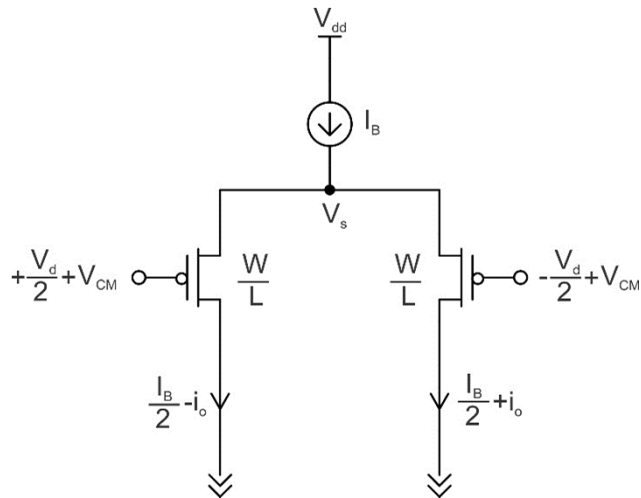
$$i_0 = \frac{v_d \sqrt{4I_B \beta \alpha - \beta^2 v_d^2}}{4\alpha}$$

$$gm = \frac{di_0}{dv_d}$$

$$gm = \frac{\beta (2\alpha I_B - \beta v_d^2)}{2\alpha \sqrt{\beta (4\alpha I_B - \beta v_d^2)}}$$

Par diferencial tipo P – Inversão Forte

Saturação



Equações do circuito

$$\beta = k_p \frac{W}{L}$$

$$\frac{I_B}{2} - i_o = \frac{\beta}{2\alpha} \left(v_s - \frac{v_d}{2} - V_{CM} - |V_T| \right)^2$$

$$\frac{I_B}{2} + i_o = \frac{\beta}{2\alpha} \left(v_s + \frac{v_d}{2} - V_{CM} - |V_T| \right)^2$$

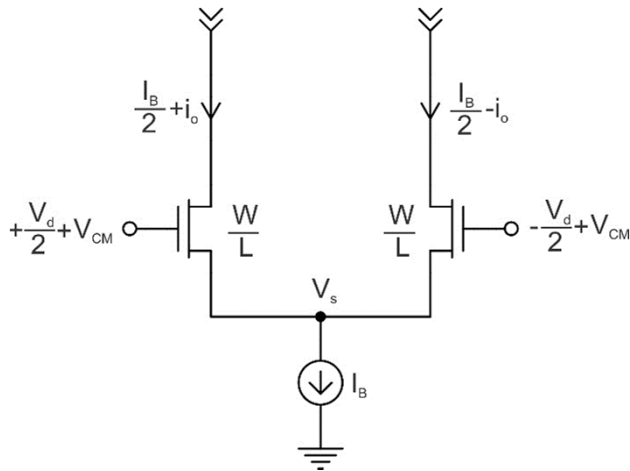
$$i_o = \frac{v_d \sqrt{4I_B \beta \alpha - \beta^2 v_d^2}}{4\alpha}$$

$$gm = \frac{di_o}{dv_d}$$

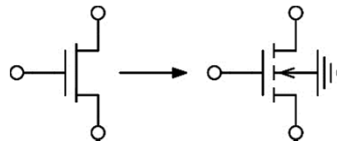
$$gm = \frac{\beta (2\alpha I_B - \beta v_d^2)}{2\alpha \sqrt{\beta (4\alpha I_B - \beta v_d^2)}}$$

Par diferencial tipo N – Inversão Fraca

Saturação



$$\left\{ \begin{array}{l} 0 \leq V_{GS} \leq V_T \\ I_{DS} = I_{D0} e^{\frac{V_{GS}-V_T}{n\phi_T}} \\ I_{D0} = \phi_T^2 k_p \frac{W}{L_{EF}} (n-1) \\ n = 1 + \frac{\gamma}{2\sqrt{2\phi_F + V_{SB}}} \\ \phi_T = \frac{k_B T}{q} \\ k_p = \mu_n C_{ox} \end{array} \right.$$



Equações do circuito

$$\frac{I_B}{2} + i_o = I_{D0} e^{\frac{\frac{v_d}{2} + V_{CM} - v_s - V_T}{n\phi_T}}$$

$$\frac{I_B}{2} - i_o = I_{D0} e^{\frac{-\frac{v_d}{2} + V_{CM} - v_s - V_T}{n\phi_T}}$$

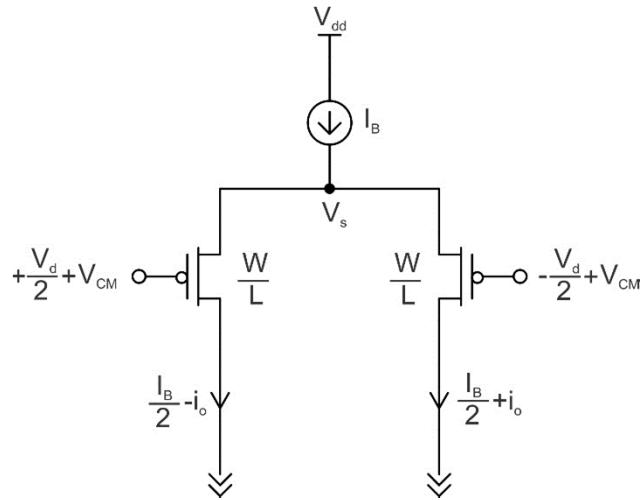
$$i_o = \frac{I_B}{2} \left(\frac{e^{\frac{v_d}{n\phi_T}} - 1}{e^{\frac{v_d}{n\phi_T}} + 1} \right) = \frac{I_B}{2} \tanh \left(\frac{v_d}{2n\phi_T} \right)$$

$$gm = \frac{di_o}{dv_d}$$

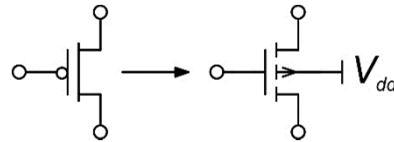
$$gm = \frac{I_B}{n\phi_T} \frac{e^{\frac{v_d}{n\phi_T}}}{\left(1 + e^{\frac{v_d}{n\phi_T}} \right)^2}$$

Par diferencial tipo P – Inversão Fraca

Saturação



$$\left\{ \begin{array}{l} 0 \leq V_{SG} \leq |V_T| \\ I_{SD} = I_{D0} e^{\frac{V_{SG} - |V_T|}{n\phi_T}} \\ I_{D0} = \phi_T^2 k_p \frac{W}{L_{EF}} (n-1) \\ n = 1 + \frac{\gamma}{2\sqrt{2\phi_F + V_{BS}}} \\ \phi_T = \frac{k_B T}{q} \\ k_p = \mu_p C_{ox} \end{array} \right.$$



Equações do circuito

$$\frac{I_B}{2} - i_o = I_{D0} e^{\frac{v_s - \frac{v_d}{2} - V_{CM} - |V_T|}{n\phi_T}}$$

$$\frac{I_B}{2} + i_o = I_{D0} e^{\frac{v_s + \frac{v_d}{2} - V_{CM} - |V_T|}{n\phi_T}}$$

$$i_o = \frac{I_B}{2} \left(\frac{e^{\frac{v_d}{n\phi_T}} - 1}{e^{\frac{v_d}{n\phi_T}} + 1} \right) = \frac{I_B}{2} \tanh \left(\frac{v_d}{2n\phi_T} \right)$$

$$gm = \frac{di_o}{dv_d}$$

$$gm = \frac{I_B}{n\phi_T} \frac{e^{\frac{v_d}{n\phi_T}}}{\left(1 + e^{\frac{v_d}{n\phi_T}} \right)^2}$$

Equações Normalizadas na Inversão Forte

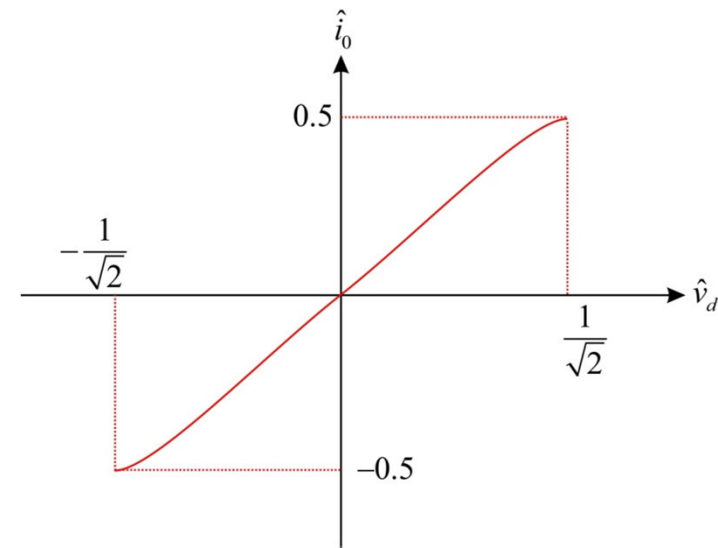
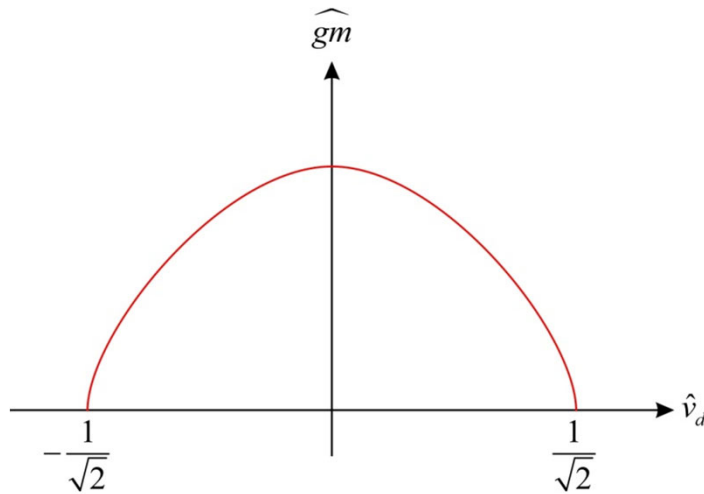
$$\hat{v}_d = \frac{v_d}{2} \sqrt{\frac{\beta}{\alpha I_B}} \quad \hat{i}_0 = \frac{i_0}{I_B} \quad \widehat{gm} = \frac{2\sqrt{\alpha}}{\sqrt{\beta I_B}} gm$$

$$\hat{i}_0 = \hat{v}_d \sqrt{1 - \hat{v}_d^2} \quad \longrightarrow \quad \widehat{gm} = \frac{(1 - 2\hat{v}_d^2)}{\sqrt{1 - \hat{v}_d^2}}$$

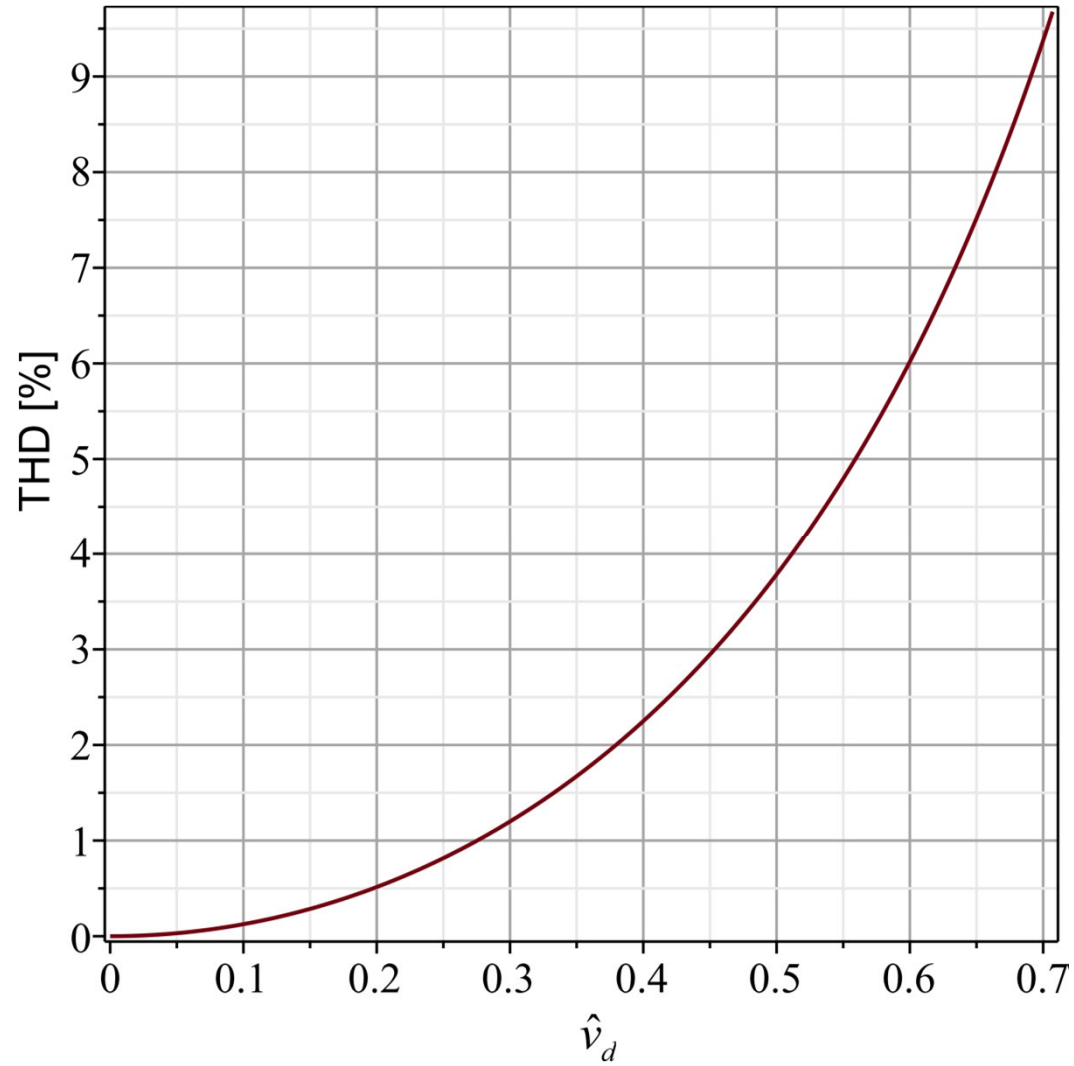
$$|\hat{v}_{d_{\max}}| = \frac{1}{\sqrt{2}} \quad \longrightarrow \quad |\hat{i}_{0_{\max}}| = \frac{1}{2} \quad \longrightarrow \quad \widehat{gm}_{\max} = 1 \quad \longrightarrow \quad \widehat{gm}_{\min} = 0$$

$$i_0 = \frac{v_d \sqrt{4I_B \beta \alpha - \beta^2 v_d^2}}{4\alpha}$$

$$gm = \frac{\beta(2\alpha I_B - \beta v_d^2)}{2\alpha \sqrt{\beta(4\alpha I_B - \beta v_d^2)}}$$



Curva de THD para a Tensão Diferencial Normalizada, THDmax=10%

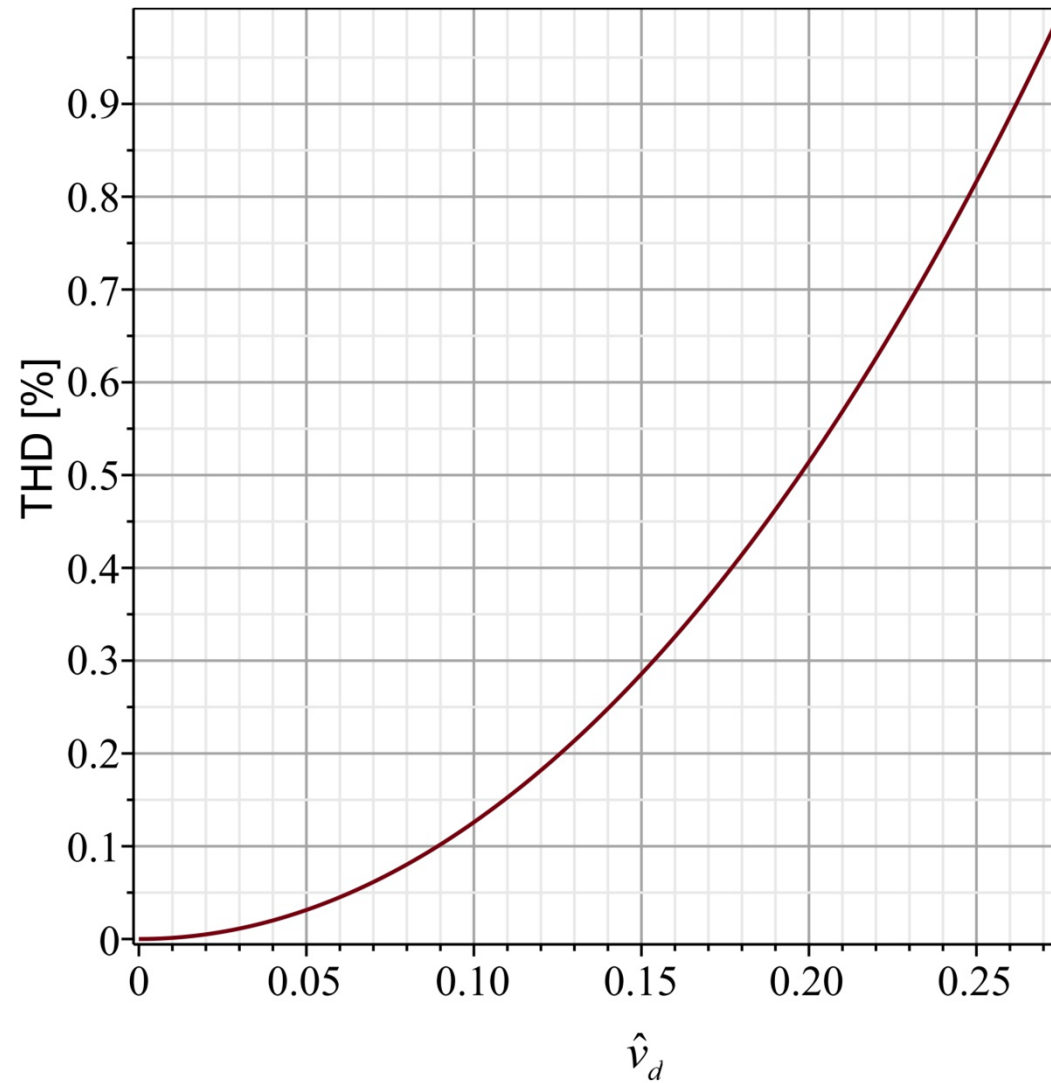


$$\hat{v}_d = \frac{v_d}{2} \sqrt{\frac{\beta}{\alpha I_B}}$$

$$\widehat{gm} = \frac{(1 - 2\hat{v}_d^2)}{\sqrt{1 - \hat{v}_d^2}}$$

$$\widehat{gm} = \frac{2\sqrt{\alpha}}{\sqrt{\beta I_B}} gm$$

Curva de THD para a $THD_{max}=1\%$



$$\hat{v}_d = \frac{v_d}{2} \sqrt{\frac{\beta}{\alpha I_B}}$$

$$\widehat{gm} = \frac{(1 - 2\hat{v}_d^2)}{\sqrt{1 - \hat{v}_d^2}}$$

$$\widehat{gm} = \frac{2\sqrt{\alpha}}{\sqrt{\beta I_B}} gm$$

Equações Normalizadas na Inversão Fraca

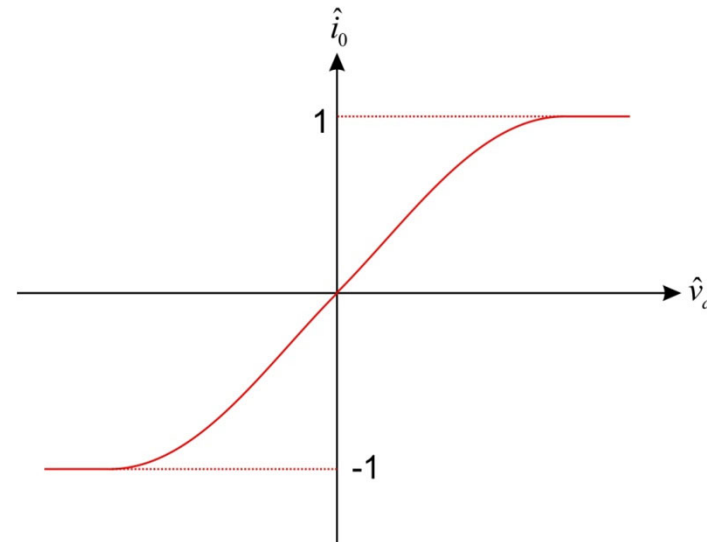
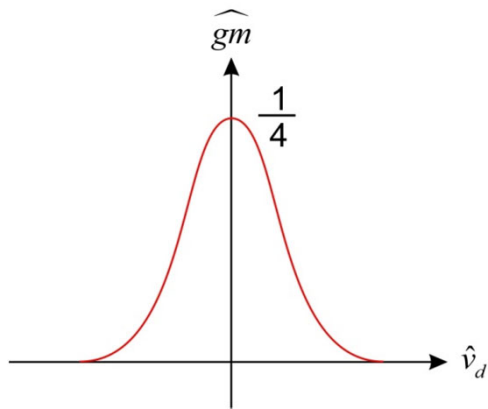
$$\hat{v}_d = \frac{v_d}{n\phi_T} \quad \hat{i}_0 = \frac{2}{I_B} i_0 \quad \widehat{gm} = \frac{n\phi_T}{I_B} gm$$

$$i_0 = \frac{I_B}{2} \left(\frac{e^{\frac{v_d}{n\phi_T}} - 1}{e^{\frac{v_d}{n\phi_T}} + 1} \right) = \frac{I_B}{2} \tanh \left(\frac{v_d}{2n\phi_T} \right)$$

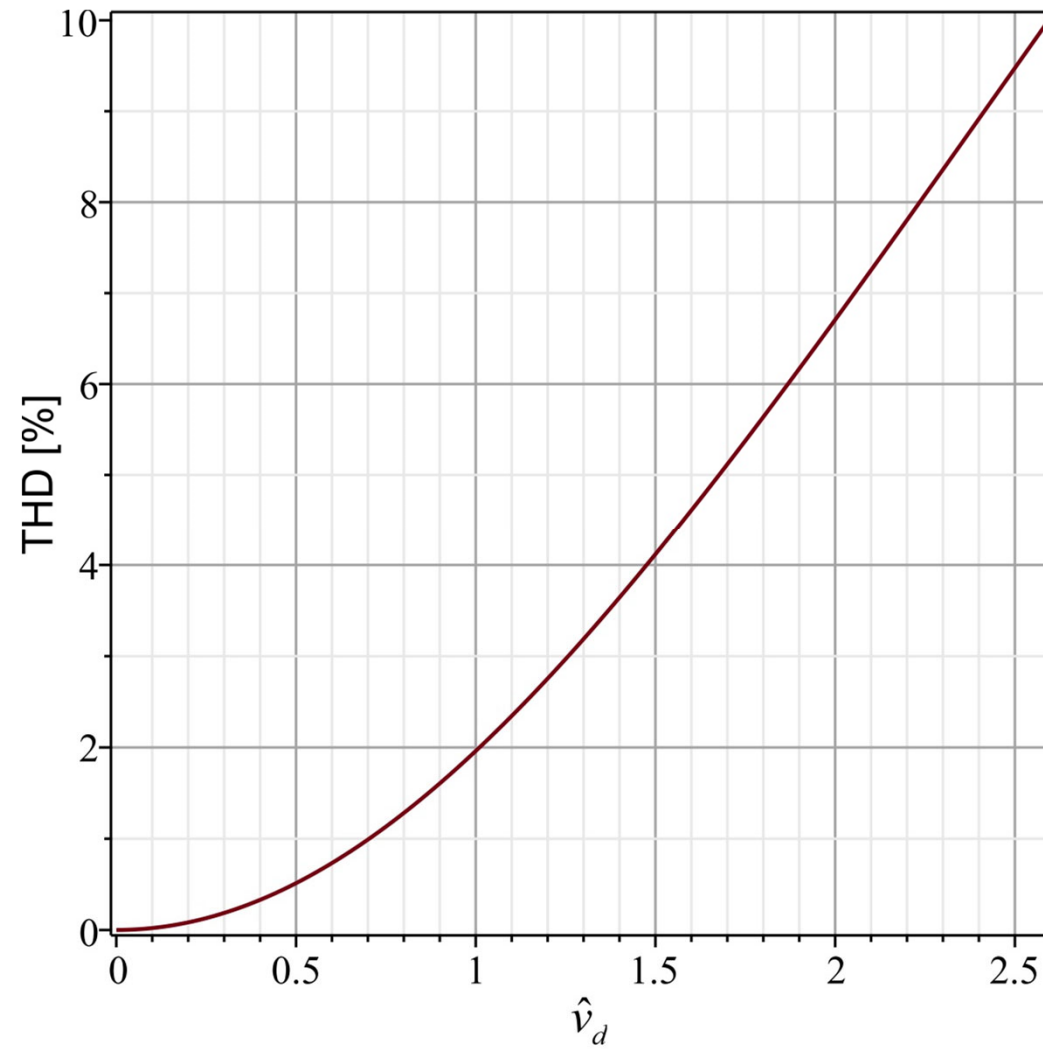
$$\hat{i}_0 = \frac{e^{\hat{v}_d} - 1}{e^{\hat{v}_d} + 1} = \tanh \left(\frac{\hat{v}_d}{2} \right) \quad \longrightarrow \quad \widehat{gm} = \frac{e^{\hat{v}_d}}{(1 + e^{\hat{v}_d})^2}$$

$$gm = \frac{I_B}{n\phi_T} \frac{e^{\frac{v_d}{n\phi_T}}}{\left(1 + e^{\frac{v_d}{n\phi_T}}\right)^2}$$

$$|\hat{i}_{0_{\max}}| = 1 \quad \longrightarrow \quad \widehat{gm}_{\max} = \frac{1}{4} \quad \longrightarrow \quad \widehat{gm}_{\min} = 0 \Big|_{|\hat{v}_d| = \infty}$$



Curva de THD para a $THD_{max}=10\%$

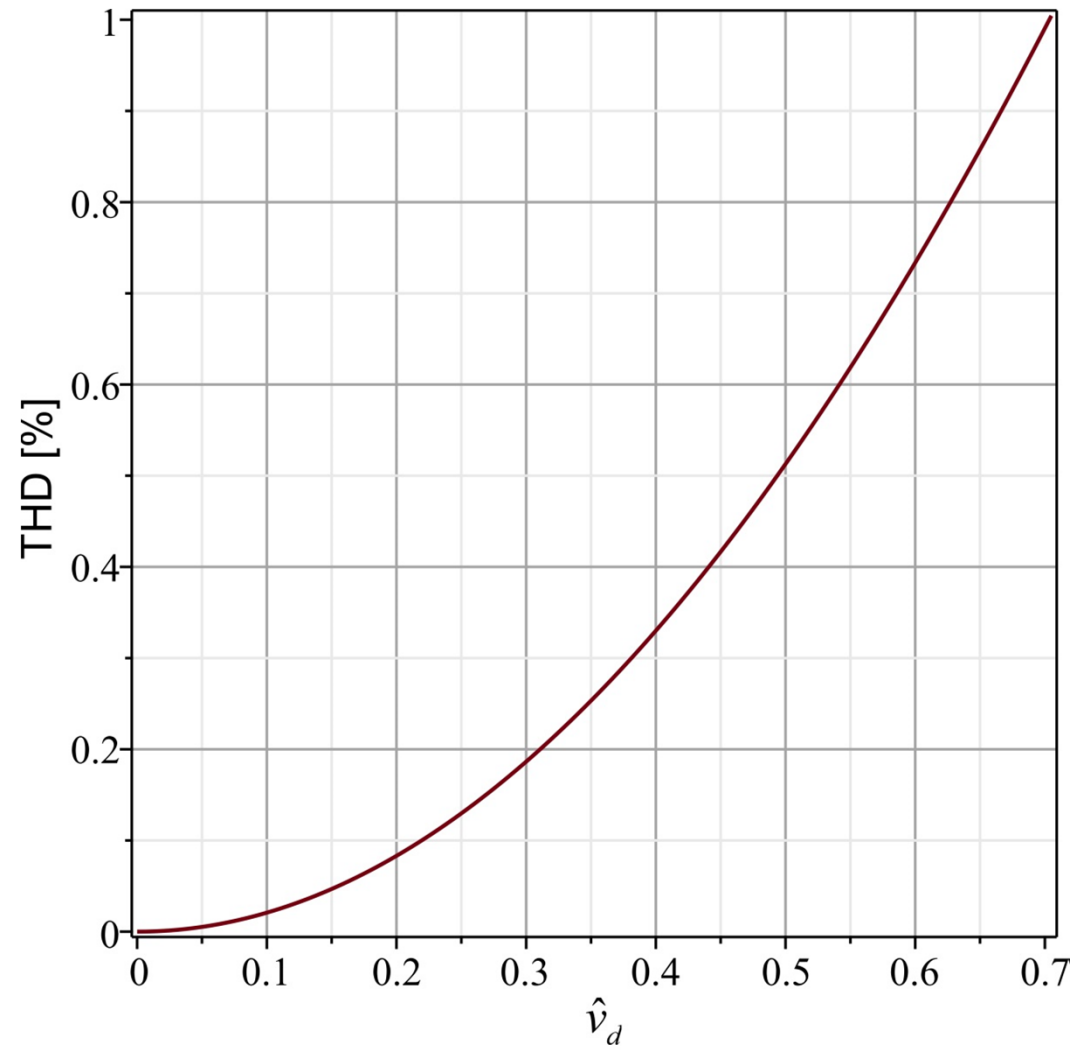


$$\hat{v}_d = \frac{v_d}{n\phi_T}$$

$$\widehat{gm} = \frac{e^{\hat{v}_d}}{(1 + e^{\hat{v}_d})^2}$$

$$\widehat{gm} = \frac{n\phi_T}{I_B} gm$$

Curva de THD para a $THD_{max}=1\%$



$$\hat{v}_d = \frac{v_d}{n\phi_T}$$

$$\widehat{gm} = \frac{e^{\hat{v}_d}}{(1 + e^{\hat{v}_d})^2}$$

$$\widehat{gm} = \frac{n\phi_T}{I_B} gm$$

**Final deste
Tópico**